

defined by the combinations of levels of function in each of 8 health attributes, including attributes potentially affected by OA: ambulation, dexterity, and pain and discomfort. Next, one attaches a utility score to each possible health state; this score describes the desirability (based on a preference survey of the general population) of the state relative to the 2 anchor states: normal health (usually assigned a utility score of one) and death (usually assigned a utility score of zero). Using the health-state classification and utility function, analysts can compare the utility value of morbidity reductions produced by several candidate interventions targeted at different populations and/or different diseases. Further, these utility values can be combined with evidence on the mortality effects of alternative interventions to rank the interventions' impact on quality-adjusted life-years (QALY). Numerous studies have examined the utility^{1,2} associated with OA^{3,4} and computed cost-utility analyses, a common approach for evaluating the economic influence of medical care technologies where effects are expressed as quality-adjusted survival, allowing for comparisons across different diseases and interventions.

Most published effectiveness studies in OA measure HRQOL using just the WOMAC. How then can the value of OA treatments be compared to the value of treatments for other conditions? One option — repeating these OA studies using a generic HRQOL measure — would be very costly. A more practical option would be to map WOMAC scores into a generic measure of HRQOL.

We attempted to map the WOMAC into HUI3 utility scores that can ultimately be used in a cost-utility analysis.

MATERIALS AND METHODS

Data source. Data came from a previously reported multicenter, open-label randomized clinical trial (RCT) of patients with OA of the knee randomized (1:1) to either "appropriate care with hylan G-F 20" (AC+H) or to "appropriate care without hylan G-F 20" (AC) and followed for one year. Appropriate care was defined by the Guidelines for the Medical Management of Osteoarthritis of the Knee proposed by the American College of Rheumatology⁵. Patients in this study had symptomatic knee OA of mild to moderate severity that was previously treated with analgesics. Appropriate care could include medications such as analgesics, nonsteroidal antiinflammatory drugs, corticosteroid injections, supportive measures such as education and counseling, weight loss, joint rest, application of heat or ice, the use of devices, physical therapy, arthroscopy, and total joint replacement. Patients randomized to the AC+H group could receive more than one course of hylan G-F 20 treatment in the study knee (i.e., the knee most symptomatic or with the most predominant musculoskeletal problem) if medically warranted, and could receive bilateral treatment if their contralateral knee was affected.

Patients were assessed by the clinical investigator at baseline and 12 months. Both WOMAC and HUI3 were measured at multiple intervals (0, 1, 2, 4, 6, 8, 10, and 12 mo) for 255 patients and were completed by telephone interview from Months 1 to 12. The results showed that hylan G-F 20, when used in conjunction with appropriate care, provides improvement in outcomes that is both clinically important and statistically significant as measured by the change in the WOMAC pain score (38% reduction with hylan G-F 20 and appropriate care vs 13% for appropriate care only; $p = 0.0001$) and HUI3 utility score (0.071 increase; $p < 0.05$)^{4,6}.

WOMAC Index. The WOMAC has been well validated^{7,8} and is widely used in clinical studies of patients with hip and knee OA of varying degrees of

severity^{8,9}. It is a valid, reliable, and responsive measure of outcome, and has been used in diverse clinical and interventional environments^{9,10}.

The WOMAC Likert 3.0 scale used in the RCT is a self-administered disease-specific HRQOL instrument that evaluates pain, mobility, and stiffness in a series of 24 questions^{9,10}. Each respondent rated the extent of his/her arthritis symptom severity or degree of restriction of usual activities on a 5 point Likert scale from 1 (none) to 5 (extreme). The WOMAC Likert 3.0 provides scores for the 3 subscales: pain (minimum 0, maximum 20; based on 5 questions), stiffness (minimum 0, maximum 8; based on 2 questions), physical function (minimum 0, maximum 68; based on 17 questions); and an aggregate total score (minimum 0, maximum 30) calculated by using a weighted average of the subscale scores. In all cases, the higher the score, the worse the disability. A full description for calculating subscale and aggregate scores is provided in the scoring manual⁹.

HUI3. The HUI3 was used in the RCT to generate health-state utility scores¹¹⁻¹³. HUI3 utility scores have interval scale properties; hence one can compute cross-sectional and time-based differences in scores. The HUI3 has been used in many clinical trials and 5 major Canadian population health surveys, providing extensive data on population norms¹⁴. The performance of the HUI3 system has been tested extensively¹⁵⁻¹⁸.

Subjects filled out the self-complete HUI3 questionnaire. This form consists of 12 questions to determine functional status in each of 8 attributes (dimensions) of health; each attribute has 5 or 6 levels of functional capacity ranging from normal function to severe disability. The 8 attributes are: vision (5 levels), hearing (6), speech (5), ambulation (6), dexterity (6), emotion (5), cognition (6), and pain and discomfort (5).

The HUI3 system includes a mapping of each 8 element health state into an overall utility score and 8 single-attribute utility scores¹⁹. The utility scoring formulas are calculated from a multiplicative multiattribute utility function based on preference measurements obtained from a random sample of the general population. Single-attribute utility scores range from 0.0 (most severe disability) to 1.0 (no disability, normal). Overall HUI3 utility scores, which are the focus of this study, range from -0.36 (the score attached to the worst HUI3 health state) to 0.0 (dead) to 1.0 (perfect health). A negative score implies a health state worse than death. Complete instructions on calculating attribute levels and utility scores are provided in the scoring manual²⁰.

Representation of WOMAC scores in the prediction model. We considered several alternative representations of the WOMAC variables for purposes of predicting HUI3 utility scores. These were: (1) responses to each of the 24 WOMAC questions represented using 4 binary indicators (producing $24 \times 4 = 96$ indicators in total) to represent the response categories: "mild," "moderate," "severe," "extreme." The response "none" was the baseline category; (2) as above, except the response categories "mild" and "moderate" were collapsed into one level, as were the response categories "severe" and "extreme." This reduced the number of indicators from 96 to 48; (3) WOMAC subscale scores: pain, stiffness, and function; (4) WOMAC subscale scores: pain, stiffness, and function and pairwise interaction terms (i.e., pain \times stiffness, pain \times function, function \times stiffness, pain², stiffness², function²) to account for possible nonlinearities; and (5) the WOMAC aggregate total score (total) and its square (total²).

Representation of demographic and clinical variables in the prediction model. Several demographic (age at baseline and sex) and clinical variables (years since onset of OA in the study knee, and Kellgren radiographic grade) were considered important in predicting utility and hence were included in the prediction model. Although these additional clinical variables should improve the predictive performance of the model, some users might not have data on these covariates. We therefore considered several specifications, which exclude some or all of these covariates: (1) no covariates; (2) demographic covariates; (3) demographic covariates + years since onset of OA in the study knee; (4) demographic covariates + years since onset of OA in the study knee + Kellgren radiographic grade; where demographic covariates = age, age², sex; years since onset of OA in the study knee = years since onset of OA, years since onset of OA²; Kellgren radiographic grade = indicators of radiographic grade I, grade II, grade III, grade IV; the radiographic grade 0 was the baseline category.

The 5 representations of the WOMAC and 4 combinations of demographic/clinical covariates yielded 20 different candidate sets of predictor variables.

Estimators. We elected to model HUI3 utility scores as a conventional linear function of the covariates. It was unclear, however, which estimation technique was appropriate, given that the models were estimated using longitudinal data. Given that our goal is prediction, and not the estimation of the individual model measures per se, ordinary least squares (OLS) should yield unbiased predictions even with longitudinal data. On the other hand, predictions might be more precise if the longitudinal nature of the data were explicitly modeled. A conventional fixed effects specification is inappropriate given that estimates are conditional on the subjects in the data, making it impossible to generalize to other subjects. A random effects (RE) specification that decomposes the model error term into a conventional subject- and measurement-specific error and a subject-specific, time-invariant error could be appropriate. We therefore considered both the OLS and RE estimators. Further details on model estimation are provided in the Appendix.

Prediction model selection. We required a method to select the “best” model from the 40 candidate prediction models (2 estimators and 20 sets of covariates). We elected to assess the models on their ability to predict the utility scores of “out-of-sample” subjects — that is, those subjects whose data were not used to estimate the models²¹. Models that fare well on this criterion are also likely to do well in routine use. The measures of each candidate model were thus estimated using a randomly chosen subset of two-thirds of the subjects; the fitted model was used to predict the HUI3 scores of the remaining one-third of the subjects. The difference between the actual and predicted HUI3 scores in the prediction subsample — the “prediction error” — was used to generate the mean absolute error (MAE), which is the average absolute prediction error²¹. The MAE was identified *a priori* as the primary criterion for model selection as it provided a directly interpretable measure of the prediction performance of individual HUI3 scores.

The MAE likely varies from sample to sample, for 2 reasons. First, it depends on the (random) division of the sample into estimation and prediction subsamples, as well as the idiosyncratic components of utility of individuals in the prediction subsample. Second, it also likely depends on the sampling error in the estimates of the model measures. Since the MAE is a random variable, we inferred the precision of our estimator of MAE from the empirical 95% confidence interval (CI) of the bootstrapped distribution of MAE. Specifically, for each candidate model, the model selection procedure (i.e., the selection of the prediction subsample, model estimation, and estimation of MAE) was repeated 500 times, thereby generating 500 MAE estimates. The model with the lowest mean MAE was selected as the preferred model.

For comparison purposes we also evaluated the predictive performance of the models using several other prediction performance statistics: (1) root mean square error (RMSE): the RMSE is the positive square root of the average squared prediction error. In contrast to the MAE, the RMSE attaches greater weight to larger errors and favors prediction models that do not produce particularly large errors at the expense of models that are off by a modest amount; (2) intraclass correlation coefficient (ICC): the ICC, a measure of agreement between subject’s predicted and observed scores, was estimated for each model from a 2-way mixed model ANOVA^{22,23}. ICC is a ratio of between-subject variance over the sum of the between-subject and within-subject variance. The ICC measure is similar to MAE in that when ICC = 1, MAE = 0. To implement the ICC, a model of the following form was estimated:

$$\text{HUI3}[ijt] = \alpha + x[t]\beta + v[i] + \epsilon[ijt]$$

where: HUI3[ijt] = HUI3 score for patient *i* at time *t* measured according to method; *j* = (actual, predicted); α , β = measures to be estimated; $x[t]$ = time indicators (to pick up systematic variation in HUI3 scores of patient *i* measured according to method *j* over time); $v[i]$ = patient-specific random effect; $\epsilon[ijt]$ = overall random effect. The total residual variance of the model was

calculated as: $\text{Var}(v[i] + \epsilon[ijt]) = \tau^2 + \sigma^2$, i.e., the total variance is the sum of a between-subject component (τ^2) and a within-subject component (σ^2). The ICC is the proportion of the total residual variance (denominator) that is due to residual variability between subjects (numerator): $\tau^2/(\tau^2 + \sigma^2)$; (3) mean error (ME), the average prediction error, reflects the accuracy of predictions of group average HUI3 utility scores.

Assessing the prediction precision of the preferred model. In addition to generating HUI3 predictions, users of the prediction model need some sense of how accurate their predictions typically are. Precision will likely vary by the value of the predicted HUI3 score, with extreme values (less than 0 and close to 1) predicted with less precision than more frequently occurring intermediate values. Precision also likely depends on whether one wants to predict mean HUI3 scores for a group of patients or HUI3 scores for individual patients. Intuitively, group-level predictions are more precise because particularly large prediction errors of individuals within the group tend to cancel each other out. Given that most users of the formula would likely be interested in group-level predictions, group-level prediction error CI for all subjects and for subjects in various ranges of the predicted HUI3 score were estimated. This was accomplished using the following procedure. Using the preferred prediction model specification, we predicted utility scores using each subject’s baseline WOMAC and other characteristics. We then computed each subject’s prediction error; this yielded a data set containing the predicted baseline HUI3 score and associated prediction error for each of the 255 subjects. Forecast precision was assessed by applying a bootstrap procedure to these data. Specifically: (1) we randomly sampled persons, with replacement, from the prediction errors of the 255 subjects, groups of size $x = (10, 25, 50, 100, 200, 400)$; (2) we computed the group mean HUI3 predictions and prediction errors; (3) we repeated steps (1) to (2) 5000 times, thereby generating a distribution of mean prediction errors for each of the 6 group sizes and for various ranges of the predicted HUI3 score. The 2.5th and 97.5th percentiles of the empirical prediction error frequency distribution were used to estimate the prediction error CI.

Finally, we assessed the fraction of absolute subject-specific prediction errors from the primary model that exceeded 0.03. For overall HUI3 scores, differences of 0.03 or more are considered to be clinically important²⁴⁻²⁶. To do so, we randomly sampled, with replacement, 10,000 prediction errors from the baseline prediction errors of the 255 subjects, and tabulated the resulting absolute prediction errors.

RESULTS

Demographics (Table 1). In the trial, 255 patients were randomized to receive appropriate care or appropriate care with hylan G-F 20. Twenty-four subjects dropped out of the study. The average age at baseline was 63.1 years, with a mean of 9.5 years since onset of OA in the study knee. Seventy percent of subjects were female. Fifty percent of subjects had Kellgren radiographic grade III or higher.

Health status at baseline (Table 2). The majority of baseline responses to each WOMAC question for each subscale fell in the moderate to severe range with representation in almost all of the “none,” “mild,” and “extreme” categories; an appendix containing a summary of the response to each WOMAC and HUI3 question at baseline is available from the author. The mean total WOMAC score was 18.03 [standard deviation (SD) = 3.95]. The WOMAC function subscale score was highest, followed by the pain and stiffness subscales scores (the higher the score, the worse the problem).

The mean overall HUI3 utility score at baseline was 0.48 (SD 0.23); the range of the HUI3 score was -0.21 to 0.92 (Table 2). Single-attribute utility scores revealed that the mean

Table 1. Baseline demographics.

Characteristic	Mean	SD
Continuous Variables (n = 255)		
Age (yrs)	63.06	9.98
Weight (kg)	86.61	19.32
Years since onset of OA in study knee	9.45	9.59
BMI	32.51	7.63
Discrete Variables (n = 255), %		
Other knee affected by OA	84.7	
Other knee requires treatment	54.1	
Joints affected by OA [R or L hip, or spine, or interphalangeal joints (hand), or thumb carpal metacarpal joint, or 1st MTP]	99.6	
Sex		
Female	70.4	
Race		
Caucasian	92	
Black	2	
Asian	3	
Other	3	
Prior surgery of the study knee	31	
Household income, \$		
0–20,000	23	
20,000–39,000	34	
40,000–59,000	21	
60,000–79,000	10	
80,000–99,000	4	
100,000+	6	
Radiographic grade		
0	3	
I	11	
II	26	
III	34	
IV	26	

BMI: body mass index = weight in kg/(height in m²). OA: osteoarthritis.

Table 2. Baseline WOMAC total and subscale scores and HUI3 utility scores.

WOMAC Scores (n = 255)	Mean (SD)
WOMAC total score	18.03 (3.95)
WOMAC subscale scores	
Pain (0 to 20)	11.64 (2.81)
Stiffness (0 to 8)	5.08 (1.46)
Function (0 to 68)	39.87 (9.25)
HUI3 Utility scores (n = 255)	
Overall	0.48 (0.23)
Single-attribute utility scores	
Vision	0.93 (0.88)
Hearing	0.93 (0.19)
Speech	0.98 (0.08)
Ambulation	0.92 (0.14)
Dexterity	0.95 (0.13)
Emotion	0.92 (0.16)
Cognition	0.92 (0.16)
Pain	0.53 (0.25)

HUI3: Health Utility Index — Mark 3.

pain utility score was the lowest (0.53) among all the 8 attributes.

Prediction model. There were 2186 observations from 255 patients with a maximum of 8 assessments each. A total of 353 observations were dropped due to missing covariates, leaving 1833 complete records.

We initially compared the OLS to RE estimators. In each specification considered, OLS forecast precision performed better than the RE forecasts using the MAE criterion. Moreover, the models in which WOMAC was represented as a function of its subscale scores (pain, stiffness, function, pain × stiffness, pain × function, stiffness × function, pain², stiffness², function²) dominated the other representations. In what follows we report the results of the OLS estimation of the 4 remaining candidate models — i.e., those distinguished by the choice of demographic and clinical covariates. The prediction performance of these models as measured by all 4 selection statistics (MAE, RMSE, ICC, and ME) is shown in Table 3. Models that included the WOMAC subscale scores and their pairwise interaction terms, as well as demographics (age, age², sex), and the years of OA in the study knee (yrs of OA, yrs of OA²) performed marginally better than did models without these covariates. The ICC and ME selection statistics favored models that also included indicators of Kellgren radiographic grade, although again differences in prediction performance were slight. This is clear from Figure 1, which displays the bootstrapped distribution for the 4 best prediction models for each selection statistic.

Table 4 reports the estimates and standard errors of the prediction model with the best MAE score. All variables were retained in the model regardless of statistical significance. This equation is:

$$\begin{aligned} \text{Predicted HUI3 utility score} = & 0.5274776 + 0.0079676 \times \\ & \text{Pain} + 0.0065111 \times \text{Stiffness} - 0.0059571 \times \text{Function} + \\ & 0.0019928 \times \text{Pain} \times \text{Stiffness} + 0.0010734 \times \text{Pain} \times \\ & \text{Function} + 0.0001018 \times \text{Stiffness} \times \text{Function} - 0.0030813 \\ & \times \text{Pain}^2 - 0.0016583 \times \text{Stiffness}^2 - 0.000243 \times \text{Function}^2 \\ & + 0.0113565 \times \text{Age in years} - 0.0000961 \times \text{Age in years}^2 \\ & - 0.0172294 \times \text{Female} - 0.0057865 \times \text{Years since onset} \\ & \text{of OA in the study knee} + 0.0001609 \times \text{Years since} \\ & \text{onset of OA in the study knee}^2 \end{aligned}$$

To illustrate, this model predicts that a 56-year-old woman with pain, stiffness, and function scores of 10, 5, and 24, respectively, who had OA for 2.5 years would have a HUI3 score of 0.68. This model accounted for 39% of the variation in HUI3 utility scores. At the group level, the absolute difference between the predicted and the actual utility scores was < 0.001 and not statistically significantly different from zero. The function subscale score was statistically significant and negative, both alone and as a higher order term in the model.

If Kellgren radiographic grade is available in addition to information on WOMAC scores, demographics, and years

Table 3. Comparison of model performance criteria.

Performance Criterion	Model	Mean	95% CI
MAE (Primary Model)	Model 3	0.1628	0.1457 to 0.1779
	Model 4	0.1638	0.1473 to 0.1797
	Model 1	0.1645	0.1486 to 0.1798
	Model 2	0.1652	0.1488 to 0.1813
RMSE	Model 3	0.2065	0.1846 to 0.2273
	Model 4	0.2083	0.1864 to 0.2294
	Model 1	0.2083	0.1872 to 0.2290
	Model 2	0.2095	0.1868 to 0.2310
ICC	Model 4	0.5572	0.4723 to 0.6262
	Model 3	0.5557	0.4696 to 0.62934
	Model 2	0.5379	0.4536 to 0.61341
	Model 1	0.5359	0.45134 to 0.6110
ME	Model 4	-0.0003	-0.0445 to 0.0441
	Model 2	-0.0005	-0.0431 to 0.0427
	Model 3	-0.0006	-0.0422 to 0.0397
	Model 1	-0.0007	-0.04421 to 0.0412

RMSE: Root mean square error; MAE: Mean absolute error; ME: mean error; ICC: Intraclass correlation coefficient. WOMAC = $f\{\text{Pain, Stiffness, Function, (Pain} \times \text{Stiffness), (Pain} \times \text{Function), (Stiffness} \times \text{Function, Pain}^2, \text{Stiffness}^2, \text{Function}^2)\}$. DEMOG = $f\{\text{Age, Age}^2, \text{Sex}\}$. YRSOA = $f\{\text{Years since onset of OA, Years since onset of OA}^2\}$. X-Ray = $f\{\text{Kellgren radiographic grade I, II, III, IV}\}$. Model 1 = WOMAC; Model 2 = WOMAC + DEMOG; Model 3 = WOMAC + DEMOG + YRSOA; Model 4 = WOMAC + DEMOG + YRSOA + X-Ray.

since onset of OA, an alternative prediction model can be applied. This alternative model (Appendix, Model 4) accounts for a similar proportion of the variation in HUI3 utility scores (40%) as the primary model and performs slightly better than the primary model on the ME criterion.

Turning next to the forecast precision of the primary model, Table 5 reports the proportion of observations for which the absolute difference between the predicted and actual baseline HUI3 utility scores exceeded 0.03, which is commonly considered to be a clinical or policy important difference²⁶. Only 10% of absolute differences were less than 0.03; the majority of differences were in excess of 0.10.

The primary model does not appear to produce sufficiently precise individual level predictions. How did it fare at predicting group-level baseline HUI3 scores? Figure 2 and Table 6 display the group-level prediction precision of the HUI3 utility scores by group size and by the size of the predicted HUI3 score. For each of the group sizes considered, most group-level predictions were between 0.4 and 0.5, although the proportion of predictions that fell between 0.4 and 0.5 increased with group size (Figure 2). Prediction errors tended to shrink with group size as well: with groups of size 10, errors range from -0.2 to +0.2. When group size is 25, almost all errors are between -0.1 and +0.1. Table 6 provides 95% prediction error CI specific to one's group size and estimated HUI3 score. For example, if the mean predicted HUI3 utility score in a group of size 25 was 0.45, then the 95% CI around the group-level prediction would be $(0.45 - 0.06)$ to $(0.45 + 0.08) = 0.39$ to 0.53; prediction error CI for group sizes between 10 and 400 can be interpolated. Note that even with 10,000 bootstrap replications, there were insufficient realiza-

tions to construct CI for all combinations of group mean predicted HUI3 values and group size.

DISCUSSION

Generic measures of HRQOL are commonly used in clinical and policy research, and are particularly useful for economic appraisal of interventions to manage diseases that reduce functional capacity. Most studies assessing health interventions in patients with OA, however, measure HRQOL using the WOMAC, which is an OA-specific HRQOL measure. Our study offers a method for estimating generic HRQOL scores from individual-level WOMAC scores collected in trials that did not collect data on generic HRQOL.

We measured generic HRQOL using HUI3 utility scores. The HUI3 prediction models explained between 39% and 40% of the variation in the HUI3 scores of subjects in our data, all of whom had mild to moderate OA of the knee. This predictive performance is moderately lower than the performance of models that predict utility scores based on the Medical Outcomes Study Short Form-36 Health Survey (SF-36) and SF-12 with ranges of performance of 47% to 55%²⁷⁻³⁰. Moreover, our models were unable to make reliable predictions on individual subject utility scores. For instance, about 90% of predictions exceeded actual HUI3 utility scores by 0.03; 0.03 is commonly held to be a clinically important difference in HUI3 scores. The average absolute prediction error was about 0.16.

Some of the prediction error can be attributed to the measurement error in the 2 instruments. The reliability of the WOMAC and HUI3 instruments is in the range of 0.72 to 0.77³¹; Cronbach's alpha for the Likert version of the

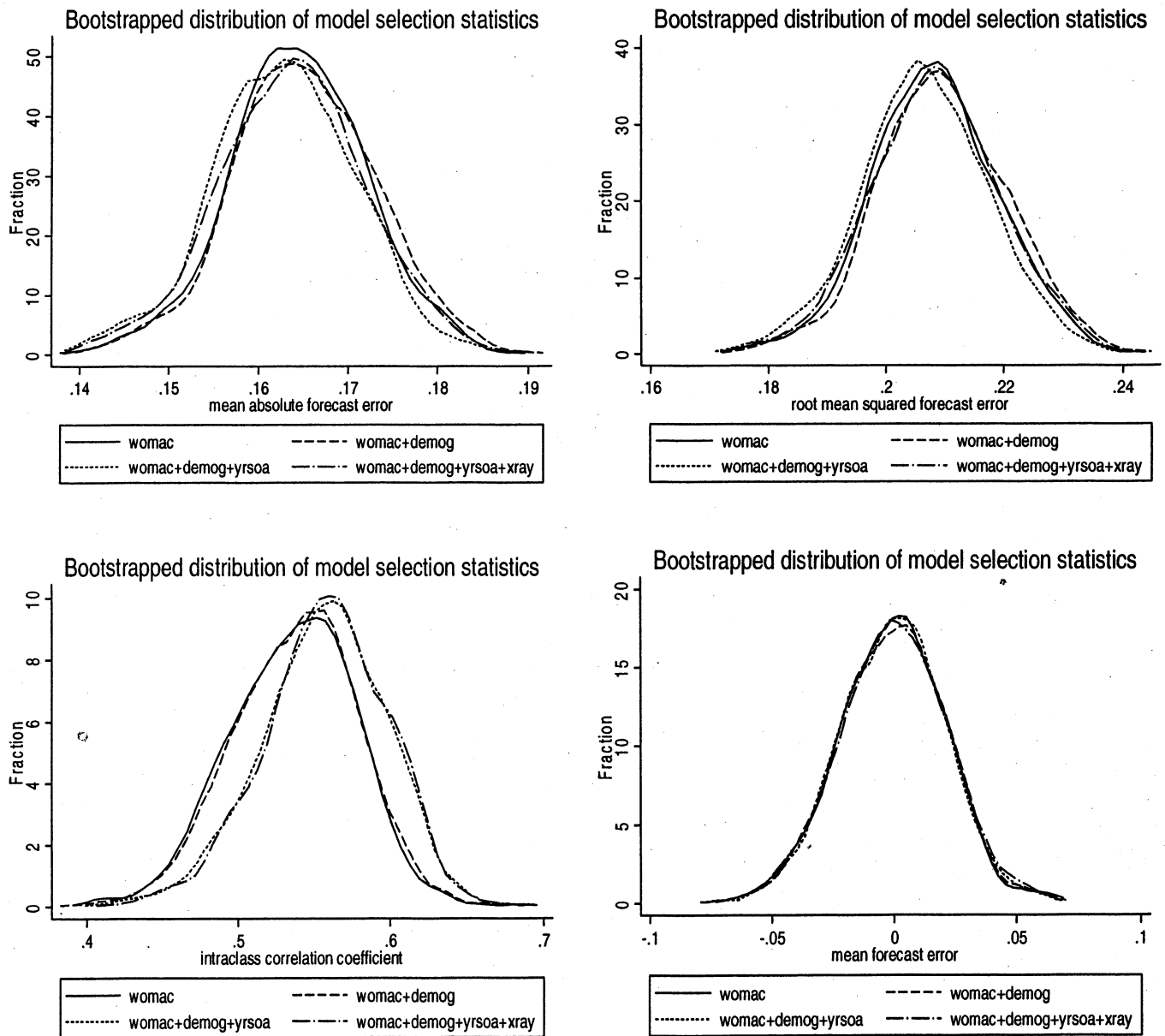


Figure 1. Bootstrapped distribution using model selection statistics MAE, RMSE, ICC, and ME. WOMAC = $f[\text{Pain, Stiffness, Function, (Pain} \times \text{Stiffness), (Pain} \times \text{Function), (Stiffness} \times \text{Function), Pain}^2, \text{Stiffness}^2, \text{Function}^2]$; DEMOG = $f[\text{Age, Age}^2, \text{Sex}]$; YRSOA = $f[\text{Yrs since onset of OA, Yrs since onset of OA}^2]$; X-RAY = $f[\text{Kellgren radiographic grade I, II, III, IV}]$.

WOMAC from the 2 original validation studies is 0.75 to 0.97^{9,10}. The majority of the prediction error, however, is likely due to the variation in HUI3 scores that is attributable to variation in vision, emotion, hearing, and other domains recorded in the HUI3 that are unaffected by OA²⁷⁻³⁰.

While the models were unable to precisely predict HUI3 scores of individual subjects, the models were able to generate reasonably precise group-average HUI3 scores. The reason is that subject-specific forecast errors tend to cancel each other out when taking the group average. We therefore recommend that the formula be used to estimate HUI3 utility scores on the basis of group average characteristics (WOMAC

scores, demographics and severity of OA). This is not overly restrictive — economic appraisal studies typically compare treatment-group-specific average HRQOL and costs.

To allow users to assess the precision of their forecasts, we have provided estimates of the forecast error and CI for various values of group average HUI3 utility score predictions and group sizes. Prediction performance for groups of patients with typical levels of dysfunction (HUI3 predictions between 0.4 and 0.6) are reasonable. For instance, the 95% CI for a group of 50 OA patients predicted to have an HUI3 score of between 0.4 and 0.6 would be about 0.10 utility units in width.

Our preferred model predicts HUI3 scores using data on

Table 4. Prediction model for estimating HUI3 scores from WOMAC (primary model).

Variable	Beta Coefficient	SE	t	p > t	95% CI
Pain	0.0080	0.0067	1.20	0.232	-0.0051 to 0.0210
Stiffness	0.0065	0.0120	0.54	0.588	-0.0171 to 0.0301
Function	-0.0060	0.0022	-2.70	0.007	-0.0103 to -0.0016
Pain × Stiffness	0.0020	0.0020	0.98	0.328	-0.0020 to 0.0060
Pain × Function	0.0010734	0.0004	2.86	0.004	0.0003 to 0.0018
Stiffness × Function	0.0001	0.0007	0.15	0.882	-0.0012 to 0.0014
Pain ²	-0.0031	0.0007	-4.42	0.000	-0.0045 to -0.0017
Stiffness ²	-0.0017	0.0025	-0.67	0.500	-0.0065 to 0.0032
Function ²	-0.0002	0.0001	-3.14	0.002	-0.0004 to -0.0001
Age	0.0114	0.0052	2.18	0.029	0.0011 to 0.0216
Age ²	-0.0001	0.00004	-2.32	0.020	-0.0002 to -0.00001
Female	-0.0172	0.0105	-1.65	0.099	-0.0377 to 0.0033
Years since onset of OA	-0.0058	0.0013	-4.36	0.000	-0.0084 to -0.0032
Years since onset of OA ²	0.0002	0.00003	4.98	0.000	0.0001 to 0.0002
Intercept	0.5275	0.1610	3.28	0.001	0.2117 to 0.8433

WOMAC Pain, Stiffness, Function, Age at baseline, and Years since onset of OA were continuous variables. Adjusted R-squared: 0.3895, SE: standard error.

Table 5. Important differences between observed and predicted HUI3 utility scores at the individual level. Predictions are from the primary prediction model reported in Table 4.

Important Difference	n = 10,000	%
Deltal		
Deltal < 0.01	494	4.9
0.01 < Deltal ≤ 0.03	499	5.0
0.03 < Deltal ≤ 0.05	856	8.6
0.05 < Deltal ≤ 0.10	1,697	17.0
Deltal > 0.10	6,454	64.5

WOMAC subscale scores, as well as their pairwise interactions, demographics, and years since onset of OA. We also report, however, several other prediction models that performed almost as well as the preferred model on the MAE criterion (or slightly better than the preferred model on the other criteria). All of these models predict HUI3 using WOMAC subscale scores and their pairwise interactions, but include as additional covariates various combinations of the demographic, years since onset of OA, and radiographic grade as additional predictors. We present these more parsimonious models

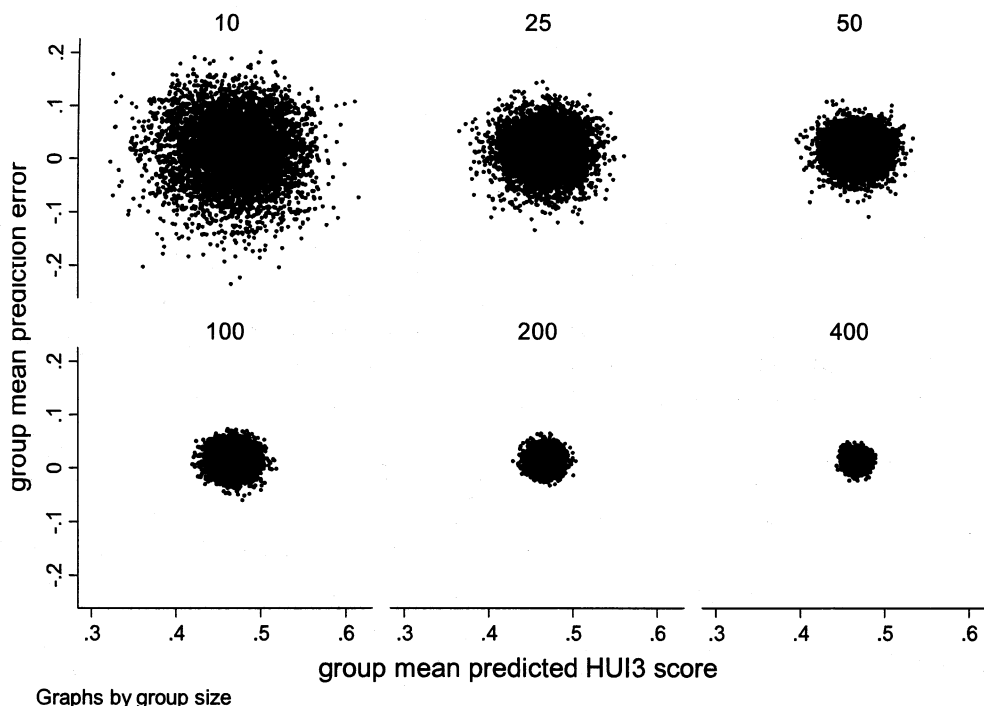


Figure 2. Group mean prediction errors, by group size (10, 25, 50, 100, 200, 400) and group mean predicted HUI3 score.

Table 6. Group level prediction precision and estimated prediction error by range of predicted HUI3 score and group size. There were no realizations for some of the combinations of predicted HUI3 score and group size.

Range of Predicted HUI3 Score	Group Size	Lower 95% CI of Forecast Error Distribution	Upper 95% CI of Forecast Error Distribution	CI Width
0.3 ≤ mean pred HUI3 < 0.4	10	-0.106	0.120	0.226
0.3 ≤ mean pred HUI3 < 0.4	25	-0.039	0.074	0.113
0.3 ≤ mean pred HUI3 < 0.4	50	0.031	0.036	0.005
0.4 ≤ mean pred HUI3 < 0.5	10	-0.103	0.125	0.228
0.4 ≤ mean pred HUI3 < 0.5	25	-0.059	0.084	0.143
0.4 ≤ mean pred HUI3 < 0.5	50	-0.037	0.065	0.102
0.4 ≤ mean pred HUI3 < 0.5	100	-0.021	0.050	0.071
0.4 ≤ mean pred HUI3 < 0.5	200	-0.011	0.040	0.051
0.4 ≤ mean pred HUI3 < 0.5	400	-0.004	0.033	0.037
0.5 ≤ mean pred HUI3 < 0.6	10	-0.105	0.114	0.218
0.5 ≤ mean pred HUI3 < 0.6	25	-0.065	0.079	0.144
0.5 ≤ mean pred HUI3 < 0.6	50	-0.042	0.065	0.107
0.5 ≤ mean pred HUI3 < 0.6	100	-0.034	0.040	0.074
0.5 ≤ mean pred HUI3 < 0.6	200	-0.014	0.017	0.031
0.6 ≤ mean pred HUI3 < 0.7	10	-0.074	0.107	0.181

for the benefit of users who lack data on these additional covariates. The group-level forecast accuracy of these more parsimonious models is very similar to the accuracy of the preferred model.

There are several limitations of our study. First, the prediction model ideally applies to patients with OA of the knee similar to patients included in the RCT from which the data were obtained. The ranges of values (minimum to maximum) for the patients in the RCT were: WOMAC pain (4 to 20), WOMAC stiffness (1 to 8), WOMAC function (13 to 66), age (40 to 87 yrs), years since onset of OA in the study knee (0.25 to 52 yrs), and radiographic grade (0 to IV). It seems likely that our results would generalize well to patients with OA of the hip and OA in general, but this remains unknown. Second, as stated earlier, the models can predict with reasonable accuracy HUI3 utility scores given group-level average WOMAC, demographic, and clinical characteristics. Predictions for individual subjects are highly inaccurate. The prediction models presented here should therefore not replace the use of a utility instrument in future clinical studies. Third, there are some concerns that the HUI3 system is not sufficiently sensitive to changes in function of the lower limbs and hands and fingers. Future research should investigate whether other generic HRQOL instruments, such as the EuroQoL^{18,20,26,32}, capture the sequelae of OA better.

With these limitations, our results offer a method for estimating health utility scores from existing WOMAC scores collected in trials where there is no other means to do so. To our knowledge, this is the first study that has attempted to establish a formula to translate WOMAC scores to HUI3 scores. Investigators who need to estimate utilities should be able to use this model for estimating QALY for decision and cost-utility analyses.

APPENDIX

Prediction models of the following form were estimated using linear regression:

$$(utility[it]^{\lambda} - 1)/\lambda = \alpha + \beta^T X[it] + \delta^T W[it] + \gamma^T Z[it] + \epsilon[it]$$

where utility[it] refers to HUI3 utility score for patient i at measurement t ; $X[it]$ is a vector of WOMAC scores; $W[it]$ is a vector of demographic variables; and $Z[it]$ is a vector of clinical variables for patient i at measurement t ; β , δ , and γ are conformable vectors of unknown measures, and $\epsilon[it]$ is a random disturbance. Only complete data were included in the regression modeling, but otherwise all observations were used for model estimation.

Equation 3 allows for utility to be transformed using the “Box-Cox” transformation: $(utility[it]^{\lambda} - 1)/\lambda$. The transformation takes on several special cases, depending on the value of λ . When $\lambda = 1$, utility remains linear; when $\lambda = -1$, the inverse value of utility results; and when $\lambda = 0$, the log of utility results. The choice of transformation was assessed by estimating λ along with the unknown model measures using a linear model incorporating a variety of different sets of covariates. The Box-Cox transformation is undefined for HUI3 scores that were not strictly positive³³; these observations were therefore removed when estimating λ . In each case, the estimated value of λ was most consistent with the linear specification ($\lambda = 1$). The HUI3 utility score therefore remained untransformed.

Prediction model for estimating HUI3 scores from WOMAC. For the convenience of users who lack information on clinical and/or demographic characteristics of subjects for whom HUI3 utility score predictions are required, we give estimates of prediction models in which these variables were removed. Model 1: WOMAC subscales with their interactions and their square terms only.

Predicted HUI3 utility score = 0.8228595 + 0.0102259 × Pain + 0.0100088 × Stiffness - 0.0074078 × Function + 0.0029179 × Pain × Stiffness + 0.0011218 × Pain × Function + 0.0000113 × Stiffness × Function - 0.0034621 × Pain² - 0.0026578 × Stiffness² - 0.0002302 × Function²

Model 2: WOMAC subscales with their interactions and their square terms as well as clinical variables of age and its second-order term and sex.

Predicted HUI3 utility score = 0.5897559 + 0.0096178 × Pain + 0.0074462 × Stiffness - 0.0068115 × Function + 0.0026835 × Pain × Stiffness + 0.0010606 × Pain × Function + 0.0001674 × Stiffness × Function - 0.0032652 × Pain² - 0.0027313 × Stiffness² - 0.0002396 × Function² + 0.0087576 × Age - 0.0000744 × Age² - 0.0251635 × Female

Model 3 (primary model): WOMAC subscales, their interactions and their square terms, age, OA duration (in the study knee) and their square terms as well as sex.

Predicted HUI3 utility score = $0.5274776 + 0.0079676 \times \text{Pain} + 0.0065111 \times \text{Stiffness} - 0.0059571 \times \text{Function} + 0.0019928 \times \text{Pain} \times \text{Stiffness} + 0.0010734 \times \text{Pain} \times \text{Function} + 0.0001018 \times \text{Stiffness} \times \text{Function} - 0.0030813 \times \text{Pain}^2 - 0.0016583 \times \text{Stiffness}^2 - 0.0002430 \times \text{Function}^2 + 0.0113565 \times \text{Age} - 0.0000961 \times \text{Age}^2 - 0.0172294 \times \text{Female} - 0.0057865 \times \text{OA duration} + 0.0001609 \times \text{OA duration}^2$

Model 4: WOMAC subscales, their interactions and their square terms, age, duration of OA (in the study knee) and their square terms as well as sex and Kellgren radiographic grade.

Predicted HUI3 utility score = $0.5044234 + 0.0084581 \times \text{Pain} + 0.0035271 \times \text{Stiffness} - 0.0054986 \times \text{Function} + 0.0021076 \times \text{Pain} \times \text{Stiffness} + 0.0010924 \times \text{Pain} \times \text{Function} + 0.0000657 \times \text{Stiffness} \times \text{Function} - 0.0031476 \times \text{Pain}^2 - 0.0012983 \times \text{Stiffness}^2 - 0.0002503 \times \text{Function}^2 + 0.0141542 \times \text{Age} - 0.0001192 \times \text{Age}^2 - 0.0212673 \times \text{Female} - 0.0055305 \times \text{OA duration} + 0.0001571 \times \text{OA duration}^2 - 0.0837873 \times \text{radiographic grade I} - 0.0458229 \times \text{grade II} - 0.0572539 \times \text{grade III} - 0.0872116 \times \text{grade IV}$

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